



#### 4.2.3.2.3 Turbo code internal interleaver

The Turbo code internal interleaver consists of bits-input to a rectangular matrix, intra-row and inter-row permutations of the rectangular matrix, and bits-output from the rectangular matrix with pruning. The bits input to the Turbo code internal interleaver are denoted by  $x_1, x_2, x_3, \dots, x_K, x_{K+1}, \dots, x_{RC}$ , where  $K$  is the integer number of the bits and takes one value of  $40 \leq K \leq 5114$ . The relation between the bits input to the Turbo code internal interleaver and the bits input to the channel coding is defined by  $x_k = o_{irk}$  for  $k=1,2,\dots,K$  and  $x_k = 0$  for  $k=K+1, K+2,\dots,RC$ , and  $K = K_i$ .

**The following section specific symbols are used in sections 4.2.3.2.3.1 – 4.2.3.4.3.3:**

$K$	Number of bits input to Turbo code internal interleaver
$R$	Number of rows of rectangular matrix
$C$	Number of columns of rectangular matrix
$p$	Prime number
$v$	Primitive root
$s(i)$	Base sequence for intra-row permutation
$q_j$	Minimum prime integers
$r_j$	Permuted prime integers
$T(j)$	Inter-row permutation pattern
$U_j(i)$	Intra-row permutation pattern
$i$	Index of matrix
$j$	Index of matrix
$k$	Index of bit sequence

##### 4.2.3.2.3.1 Bits-input to rectangular matrix

The bit sequence input to the Turbo code internal interleaver  $x_k$  is written into the rectangular matrix as follows:

(1) Determine the number of rows  $R$  of the rectangular matrix such that

$$R = \begin{cases} 5, & \text{if } (40 \leq K \leq 159) \\ 10, & \text{if } ((160 \leq K \leq 200) \text{ or } (481 \leq K \leq 530)) \\ 20, & \text{if } (K = \text{any other value}) \end{cases}$$

where the rows of rectangular matrix are numbered  $0, 1, 2, \dots, R - 1$  from top to bottom.

(2) Determine the number of columns  $C$  of rectangular matrix such that

if  $(481 \leq K \leq 530)$  then

$$p = 53 \text{ and } C = p.$$

else

Find minimum prime  $p$  such that

$$(p + 1) - K/R \geq 0,$$

and determine  $C$  such that

if  $(p - K/R \geq 0)$  then

if  $(p - 1 - K/R \geq 0)$  then

$$C = p - 1.$$

else

$$C = p.$$

end if

else

$$C = p + 1$$

end if

end if

where the columns of rectangular matrix are numbered  $0, 1, 2, \dots, C - 1$  from left to right.

(3) Write the input bit sequence  $x_k$  into the  $R \times C$  rectangular matrix row by row starting with bit  $x_1$  in column 0 of

row 0:

$$\begin{bmatrix} x_1 & x_2 & x_3 & \dots & x_C \\ x_{(C+1)} & x_{(C+2)} & x_{(C+3)} & \dots & x_{2C} \\ \vdots & \vdots & \vdots & \dots & \vdots \\ x_{((R-1)C+1)} & x_{((R-1)C+2)} & x_{((R-1)C+3)} & \dots & x_{RC} \end{bmatrix}$$

#### 4.2.3.2.3.2 Intra-row and inter-row permutations

After the bits-input to the  $R \times C$  rectangular matrix, the intra-row and inter-row permutations are performed by using the following algorithm:

(1) Select a primitive root  $v$  from table 2.

(2) Construct the base sequence  $s(i)$  for intra-row permutation as

$$s(i) = [v \times s(i - 1)] \bmod p, \quad i = 1, 2, \dots, (p - 2), \text{ and } s(0) = 1.$$

(3) Selection of the consecutive minimum prime integers: assign Let  $q_0 = 1$  be the first term prime integer in  $\{q_j\}$ , and then select the consecutive minimum prime integers  $\{q_j\}$  to be a least prime number ( $j = 1, 2, \dots, R - 1$ ) such that

$$\text{g.c.d}\{q_j, p - 1\} = 1, \quad q_j > 6, \text{ and } q_j > q_{(j-1)}, \text{ for each } j = 1, 2, \dots, R - 1,$$

where g.c.d. is greatest common divisor.

(4) Permute  $\{q_j\}$  to make  $\{r_j\}$  such that

$$r_{T(j)} = q_j, \quad j = 0, 1, \dots, R - 1,$$

where  $T(j)$  indicates the original row position of the  $j$ -th permuted row, and  $T(j)$  is the inter-row permutation pattern defined as the one of the following four kind of patterns:  $Pat_1, Pat_2, Pat_3$  and  $Pat_4$  depending on the number of input bits  $K$ .

$$T(j) = \begin{cases} Pat_4 & \text{if } (40 \leq K \leq 159) \\ Pat_3 & \text{if } (160 \leq K \leq 200) \\ Pat_1 & \text{if } (201 \leq K \leq 480) \\ Pat_3 & \text{if } (481 \leq K \leq 530) \\ Pat_1 & \text{if } (531 \leq K \leq 2280) \\ Pat_2 & \text{if } (2281 \leq K \leq 2480) \\ Pat_1 & \text{if } (2481 \leq K \leq 3160) \\ Pat_2 & \text{if } (3161 \leq K \leq 3210) \\ Pat_1 & \text{if } (3211 \leq K \leq 5114) \end{cases} ,$$

where  $Pat_1$ ,  $Pat_2$ ,  $Pat_3$  and  $Pat_4$  have the following patterns respectively.

$Pat_1$ : {19, 9, 14, 4, 0, 2, 5, 7, 12, 18, 10, 8, 13, 17, 3, 1, 16, 6, 15, 11}

$Pat_2$ : {19, 9, 14, 4, 0, 2, 5, 7, 12, 18, 16, 13, 17, 15, 3, 1, 6, 11, 8, 10}

$Pat_3$ : {9, 8, 7, 6, 5, 4, 3, 2, 1, 0}

$Pat_4$ : {4, 3, 2, 1, 0}

(5) Perform the  $j$ -th ( $j = 0, 1, 2, \dots, R - 1$ ) intra-row permutation as

if ( $C = p$ ) then

$$U_j(i) = s([i \times r_j] \bmod (p - 1)), \quad i = 0, 1, 2, \dots, (p - 2), \text{ and } U_j(p - 1) = 0,$$

where  $U_j(i)$  is the input bit position of  $i$ -th output after the permutation of  $j$ -th row.

end if

if ( $C = p + 1$ ) then

$$U_j(i) = s([i \times r_j] \bmod (p - 1)), \quad i = 0, 1, 2, \dots, (p - 2), \text{ and } U_j(p - 1) = 0, \text{ and } U_j(p) = p,$$

where  $U_j(i)$  is the input bit position of  $i$ -th output after the permutation of  $j$ -th row, and

if ( $K = C \times R$ ) then

Exchange  $U_{R-1}(p)$  with  $U_{R-1}(0)$ .

end if

end if

if ( $C = p - 1$ ) then

$$U_j(i) = s([i \times r_j] \bmod (p - 1)) - 1, \quad i = 0, 1, 2, \dots, (p - 2),$$

where  $U_j(i)$  is the input bit position of  $i$ -th output after the permutation of  $j$ -th row.

end if

**Table 2: Table of prime  $p$  and associated primitive root  $v$** 

$p$	$v$	$p$	$v$	$p$	$v$	$p$	$v$	$p$	$v$
7	3	47	5	101	2	157	5	223	3
11	2	53	2	103	5	163	2	227	2
13	2	59	2	107	2	167	5	229	6
17	3	61	2	109	6	173	2	233	3
19	2	67	2	113	3	179	2	239	7
23	5	71	7	127	3	181	2	241	7
29	2	73	5	131	2	191	19	251	6
31	3	79	3	137	3	193	5	257	3
37	2	83	2	139	2	197	2		
41	6	89	3	149	2	199	3		
43	3	97	5	151	6	211	2		

#### 4.2.3.2.3.3 Bits-output from rectangular matrix with pruning

After intra-row and inter-row permutations, the bits of the permuted rectangular matrix are denoted by  $y'_k$ :

$$\begin{bmatrix} y'_1 & y'_{(R+1)} & y'_{(2R+1)} & \cdots & y'_{((C-1)R+1)} \\ y'_2 & y'_{(R+2)} & y'_{(2R+2)} & \cdots & y'_{((C-1)R+2)} \\ \vdots & \vdots & \vdots & \cdots & \vdots \\ y'_R & y'_{2R} & y'_{3R} & \cdots & y'_{CR} \end{bmatrix}$$

The output of the Turbo code internal interleaver is the bit sequence read out column by column from the intra-row and inter-row permuted  $R \times C$  matrix starting with bit  $y'_1$  in row 0 of column 0 and ending with bit  $y'_{CR}$  in row  $R - 1$  of column  $C - 1$ . The output is pruned by deleting bits that were not present in the input bit sequence,  $O_{irk}$  to the channel coding, i.e. bits  $y'_k$  that corresponds to bits  $x_k$  with  $k > K$  are removed from the output. The bits output from Turbo code internal interleaver are denoted by  $x'_1, x'_2, \dots, x'_K$ , where  $x'_1$  corresponds to the bit  $y'_k$  with smallest index  $k$  after pruning,  $x'_2$  to the bit  $y'_k$  with second smallest index  $k$  after pruning, and so on. The number of bits output from Turbo code internal interleaver is  $K$  and the total number of pruned bits is

$$R \times C - K.$$